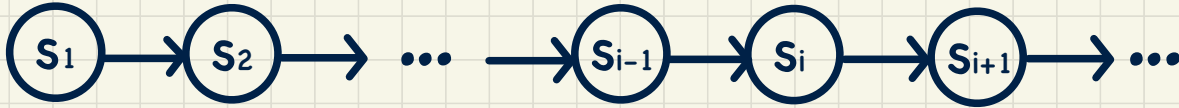


## Path Satisfaction: Temporal Operations (4)

$$\pi \models \phi_1 \text{ U } \phi_2$$

There is some future state satisfies  $\phi_2$ , and until then, all states satisfy  $\phi_1$  .



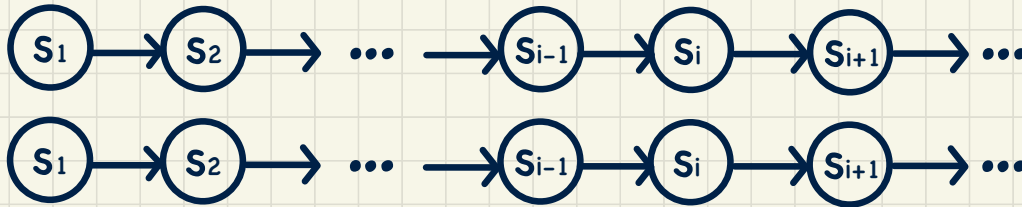
Formulation (over a path)

## Path Satisfaction: Temporal Operations (5)

$$\pi \models \phi_1 \mathbf{W} \phi_2$$

If there is ever a future state that satisfies  $\phi_2$ , then until then, all states satisfy  $\phi_1$ .

Or,  $\phi_1$  must always be the case.



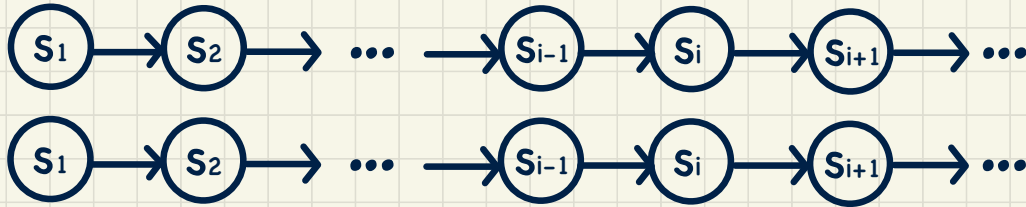
Formulation (over a path)

## Path Satisfaction: Temporal Operations (6)

$$\pi \models \phi_1 \mathbf{R} \phi_2$$

If there is ever a future state that satisfies  $\phi_1$ , then until then, all states satisfy  $\phi_2$ .

Or,  $\phi_2$  must always hold (i.e., never released).



Formulation (over a path)

# Formulating Natural Language in LTL (1)

## Natural Language:

I had smoked until I was 22.

Atom **t**: I was 22

Atom **s**: I smoke

Q. Is **s U t** an appropriate formulation?

$$\pi \models \phi_1 \mathbf{U} \phi_2 \iff \left( \exists i \bullet i \geq 1 \wedge \left( \begin{array}{l} \pi^i \models \phi_2 \\ \wedge \\ (\forall j \bullet 1 \leq j \leq i-1 \Rightarrow \pi^j \models \phi_1) \end{array} \right) \right)$$

## Formulating **Natural Language** in **LTL** (2.1)

### Natural Language:

It's impossible to reach a state  
where the system is started but not ready.

### Assumed atoms:

- started
- ready

## LTL Formulation

## Formulating Natural Language in LTL (2.2)

### Natural Language:

Whenever a request is made,  
it will be acknowledged eventually.

### Assumed atoms:

- requested
- acknowledged

### LTL Formulation

## Formulating Natural Language in LTL (2.3)

### Natural Language:

An elevator traveling upwards at the 2nd floor  
does not change its direction  
when it has passengers wishing to to to the 5th floor.

### Assumed atoms:

- floor2, floor5
- directionUp
- buttonPressed5

### LTL Formulation